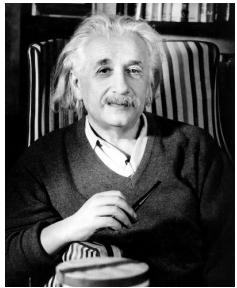


Physics of Quantum Information

Lecture 3: Entanglement (I)

The Einstein – Bohr debate: a philosophical one?



A. Einstein

Measure on A can not influence the one on B = **LOCALITY**
⇒ correlations possible only if the two photons share a **common property** which **determines their state before the measurement**

But... No such property in quantum theory

MAY 15, 1935

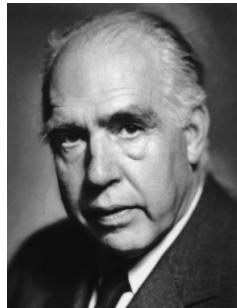
PHYSICAL REVIEW

VOLUME 47

Can Quantum-Mechanical Description of Physical Reality Be Considered Complete?

A. EINSTEIN, B. PODOLSKY AND N. ROSEN, *Institute for Advanced Study, Princeton, New Jersey*

(Received March 25, 1935)



N. Bohr

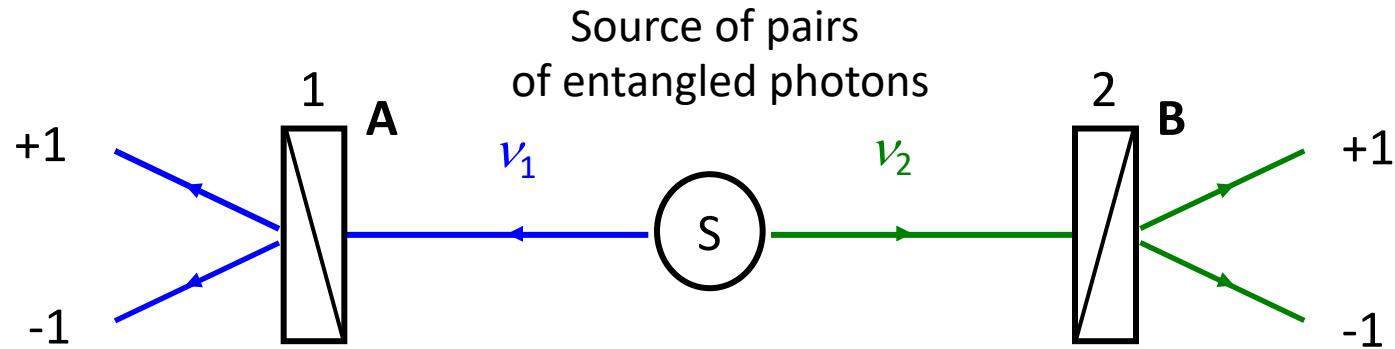
Photons have no defined polarization state before the measurement
Correlation = **intrinsic property of the state**

Polarisation state **fixed when measuring (Random result)**
Quantum physics is **complete !**

John Bell (1964): philosophical debate testable experimentally



John Bell
(1938 - 1990)



Two orientations $\mathbf{A}_1, \mathbf{A}_2$ & $\mathbf{B}_1, \mathbf{B}_2$ of each polarizer

$$\text{Measure } S = \langle \mathbf{A}_1 (\mathbf{B}_1 + \mathbf{B}_2) \rangle + \langle \mathbf{A}_2 (\mathbf{B}_1 - \mathbf{B}_2) \rangle$$

Einstein : hidden variable λ determines outcome of measurement

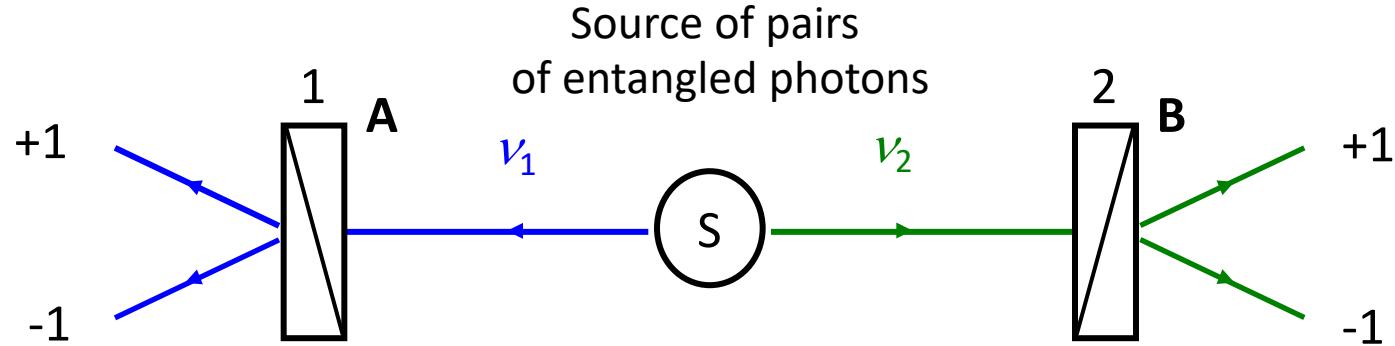
$$\mathbf{A}_1(\lambda), \mathbf{A}_2(\lambda), \mathbf{B}_1(\lambda), \mathbf{B}_2(\lambda) = \pm 1 \Rightarrow -2 \leq S \leq 2$$

Quantum Physics predicts $S > 2$ for some orientations

John Bell (1964): philosophical debate testable experimentally



John Bell
(1938 - 1990)



Two orientations $\mathbf{A}_1, \mathbf{A}_2$ & $\mathbf{B}_1, \mathbf{B}_2$ of each polarizer

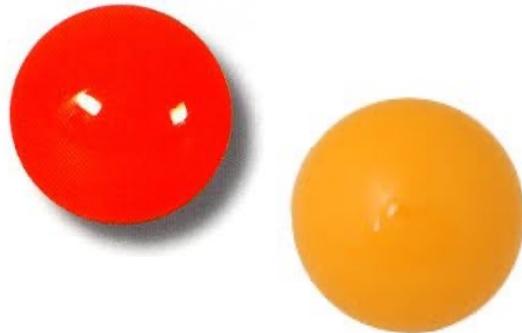
$$\text{Measure } S = \langle \mathbf{A}_1 (\mathbf{B}_1 + \mathbf{B}_2) \rangle + \langle \mathbf{A}_2 (\mathbf{B}_1 - \mathbf{B}_2) \rangle$$

Einstein : hidden variable λ determines outcome of measurement

$$\mathbf{A}_1(\lambda), \mathbf{A}_2(\lambda), \mathbf{B}_1(\lambda), \mathbf{B}_2(\lambda) = \pm 1 \Rightarrow -2 \leq S \leq 2$$

Quantum Physics predicts $S > 2$ for some orientations

Strong correlations also exist in the classical world...

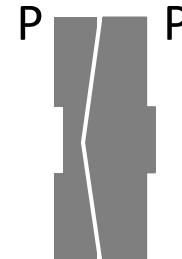
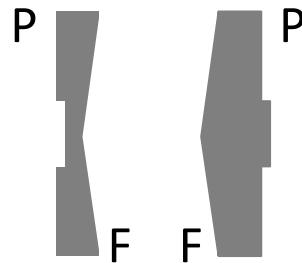


Entanglement \Rightarrow RJ, JR, RJ, RJ, JR...

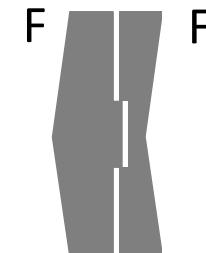


Entanglement \Rightarrow PP, FF, FF, PP, PP, FF, ...

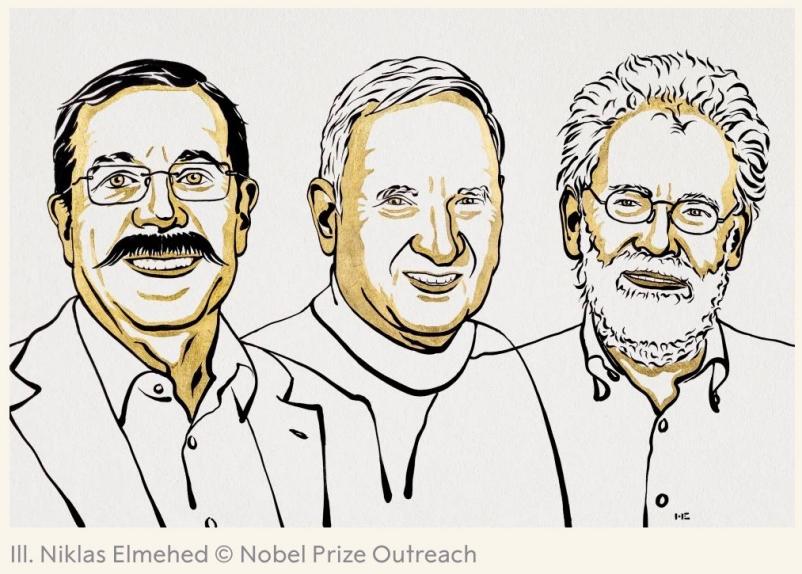
Correlations may be explained by the **random fluctuations** of a **hidden « mechanism »**



OR



The Nobel Prize in Physics 2022



The Nobel Prize in Physics 2022 was awarded jointly to Alain Aspect, John F. Clauser and Anton Zeilinger "for experiments with *entangled* photons, establishing the *violation of Bell inequalities* and pioneering *quantum information* science"

The first conclusive test: John Clauser

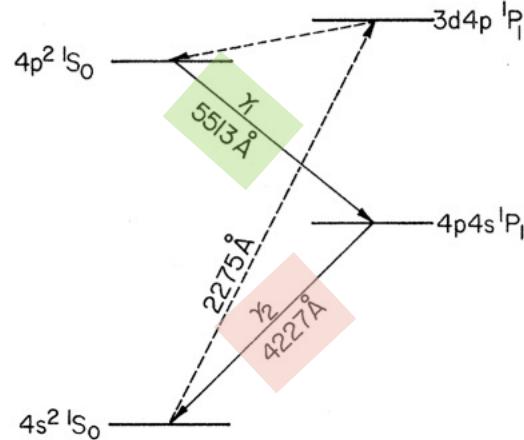
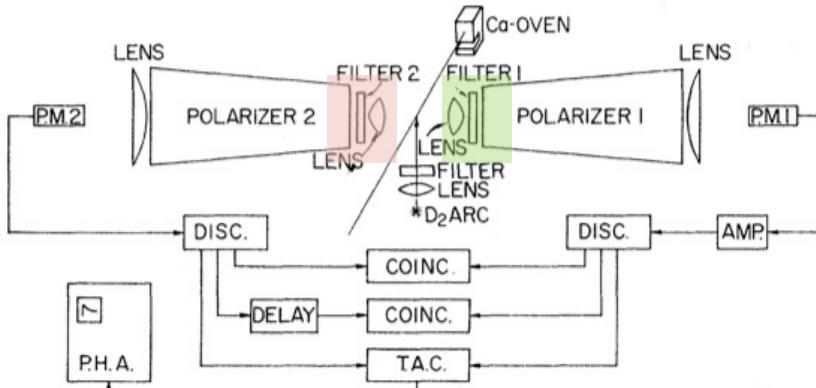


John Clauser

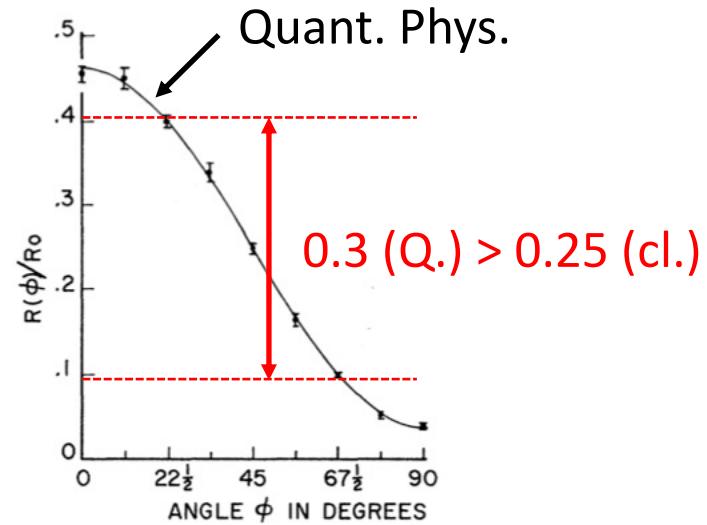


Single-photon source:
radiative cascade ${}^{40}\text{Ca}$

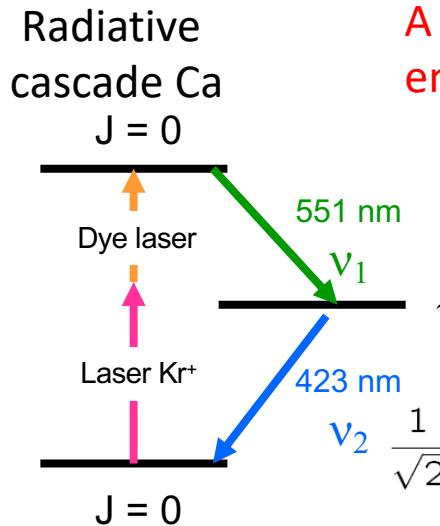
$$\frac{1}{\sqrt{2}}(|h_1, h_2\rangle + |v_1, v_2\rangle)$$



Phys. Rev. Lett. 1972

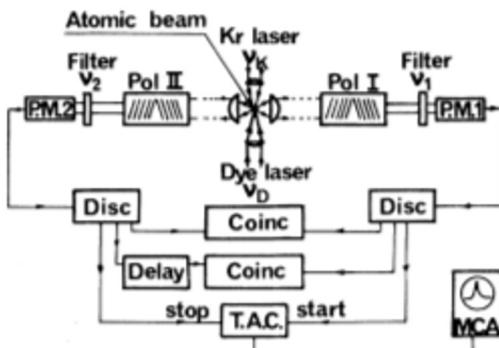
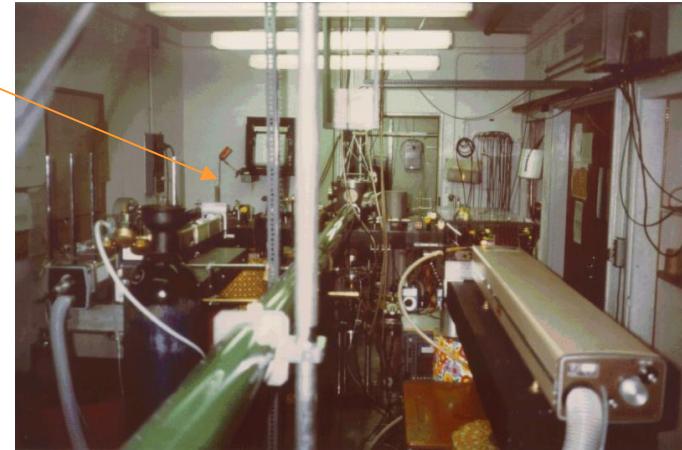


The Aspect's experiments (Orsay 1974 - 1982): exp. 1

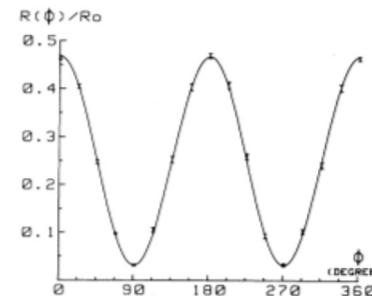


A new source of entangled photons

Aspect, Grangier & Roger, Phys. Rev. Lett. **47**, 460 (1981)



Higher flux \Rightarrow better statistics



$$\delta_{\text{exp}} = 0.0572 \pm 0.0043$$

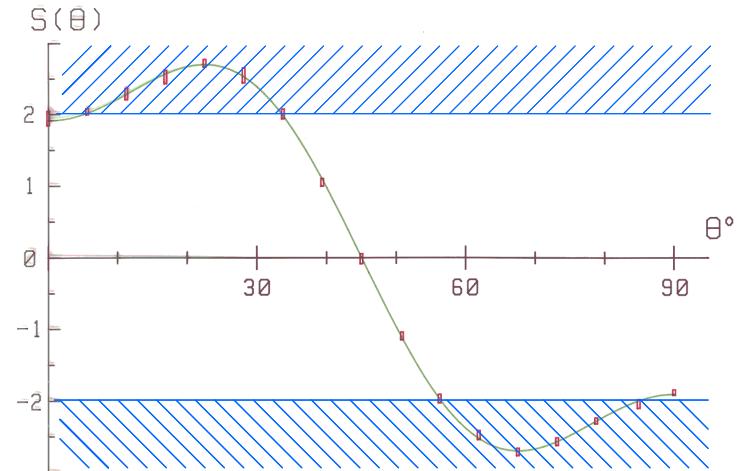
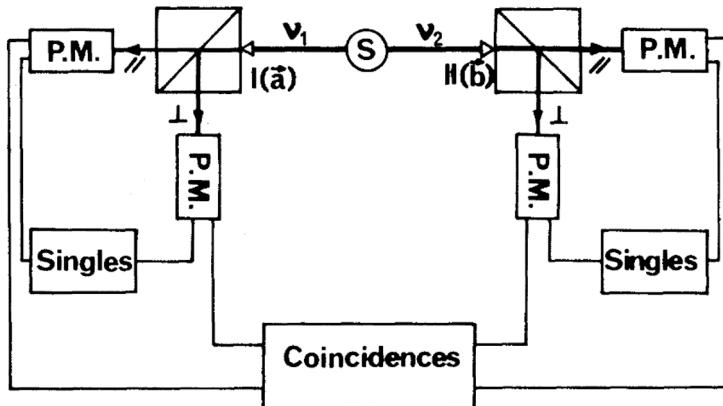
Violation by 10 standard deviations

The Aspect's experiments (Orsay 1974 - 1982): exp. 2



Aspect, Grangier & Roger, Phys. Rev. Lett. **49**, 91 (1982)

Two-channel detectors



$$-2 \leq S_{Bell} \leq 2$$

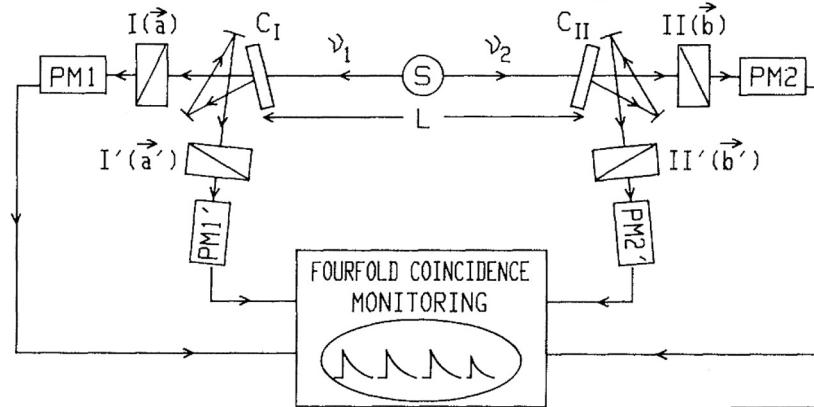
$$S_{QM}(\theta = 22.5^\circ) \leq 2.70 \pm 0.05$$
$$S_{exp}(\theta = 22.5^\circ) \leq 2.697 \pm 0.015$$

The Aspect's experiments (Orsay 1974 - 1982): exp. 3

Aspect, Dalibard & Roger, Phys. Rev. Lett. **49**, 1804 (1982)



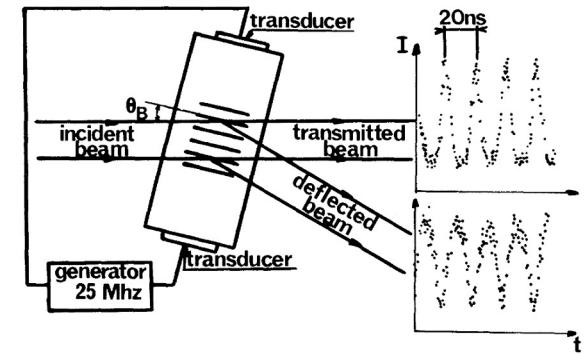
Test of non-locality



$-1 \leq S'_{Bell} \leq 0$ (Shimony-Holt inequality)

$$S'_{QM}(\theta = 22.5^\circ) = 0.112$$

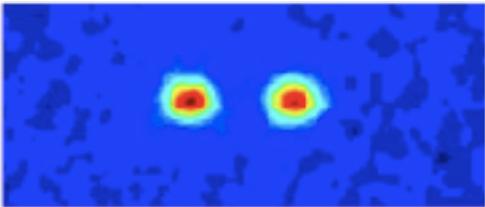
$$S'_{\text{exp}}(\theta = 22.5^\circ) = 0.101 \pm 0.020$$



And since then...

2001: 2 ions

Wineland (USA)

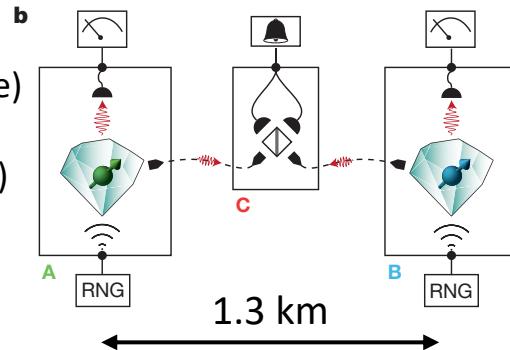


2015: « loophole-free » tests



Zeilinger (Autriche)

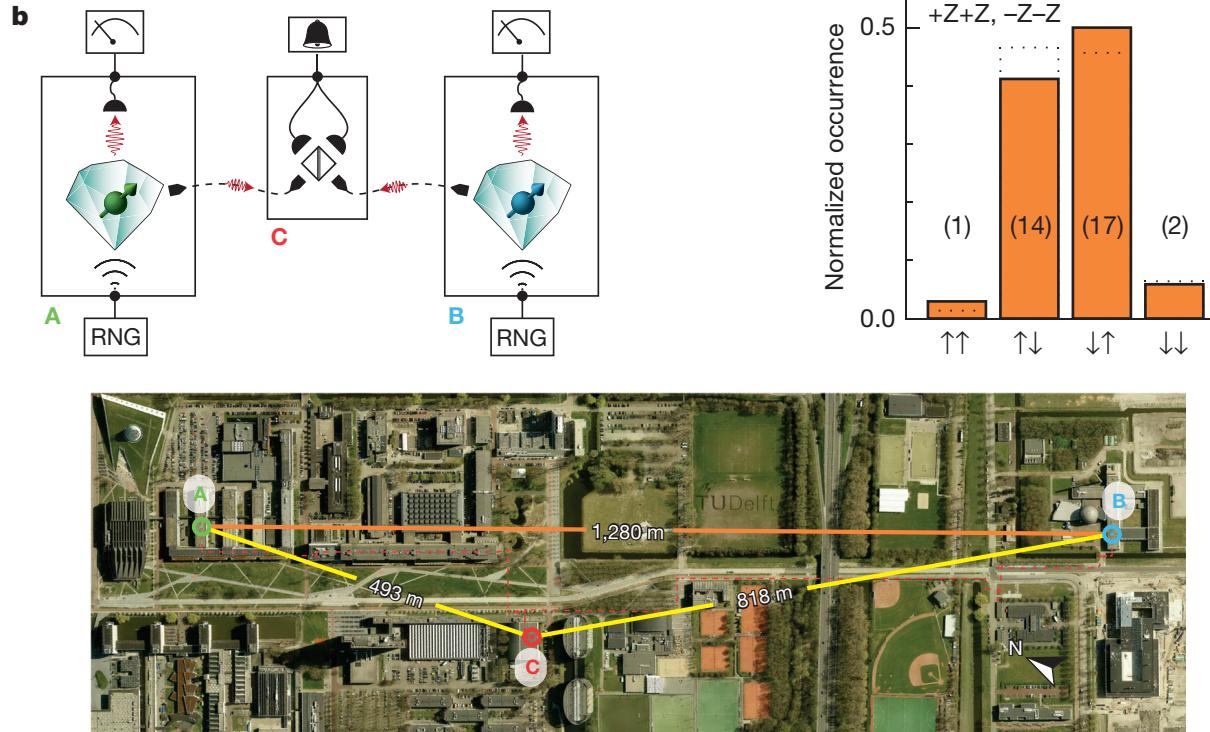
Hanson (Pays-bas)
Shalm (USA)



2017: sources in satellite
 $D = 1200 \text{ km}$

Loophole-free Bell inequality violation using electron spins separated by 1.3 kilometres

B. Hensen^{1,2}, H. Bernien^{1,2,†}, A. E. Dréau^{1,2}, A. Reiserer^{1,2}, N. Kalb^{1,2}, M. S. Blok^{1,2}, J. Ruitenberg^{1,2}, R. F. L. Vermeulen^{1,2}, R. N. Schouten^{1,2}, C. Abellán³, W. Amaya³, V. Pruneri^{3,4}, M. W. Mitchell^{3,4}, M. Markham⁵, D. J. Twitchen⁵, D. Elkouss¹, S. Wehner¹, T. H. Taminiau^{1,2} & R. Hanson^{1,2}



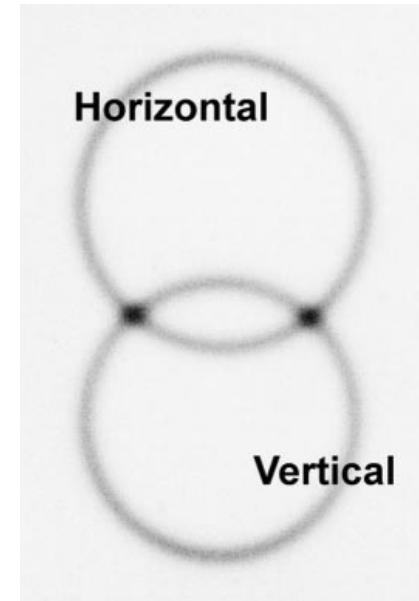
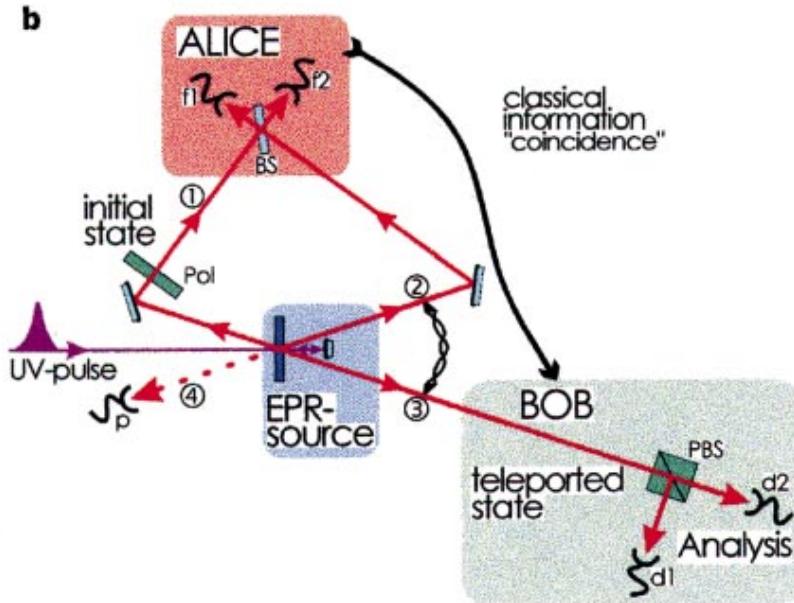
Quantum teleportation with photons

Experimental quantum teleportation

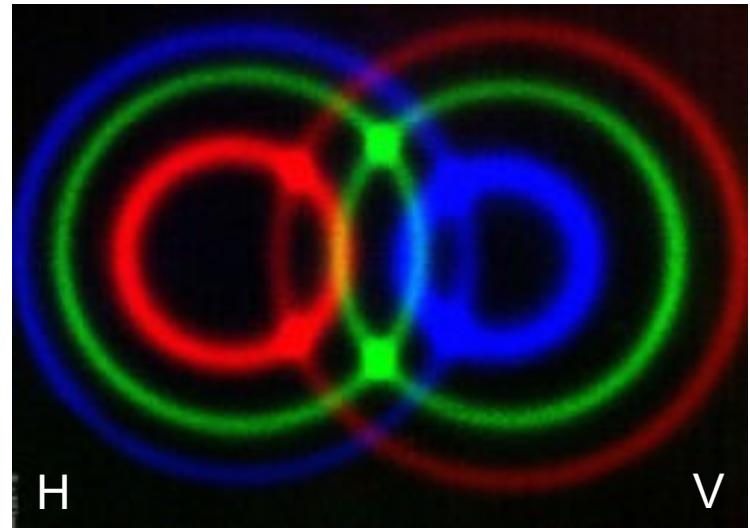
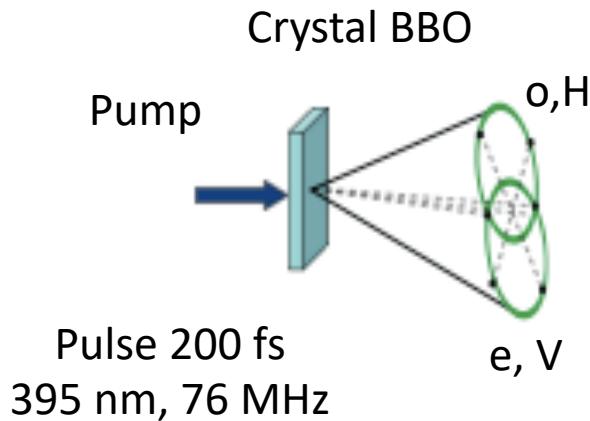
Nature 1997

Dik Bouwmeester, Jian-Wei Pan, Klaus Mattle, Manfred Eibl, Harald Weinfurter & Anton Zeilinger

Institut für Experimentalphysik, Universität Innsbruck, Technikerstr. 25, A-6020 Innsbruck, Austria



Spontaneous parametric downconversion (type II)



Proba to create 1 pair $\sim 10^{-2}$

$$\frac{1}{\sqrt{2}}(|H, V\rangle + |V, H\rangle)$$

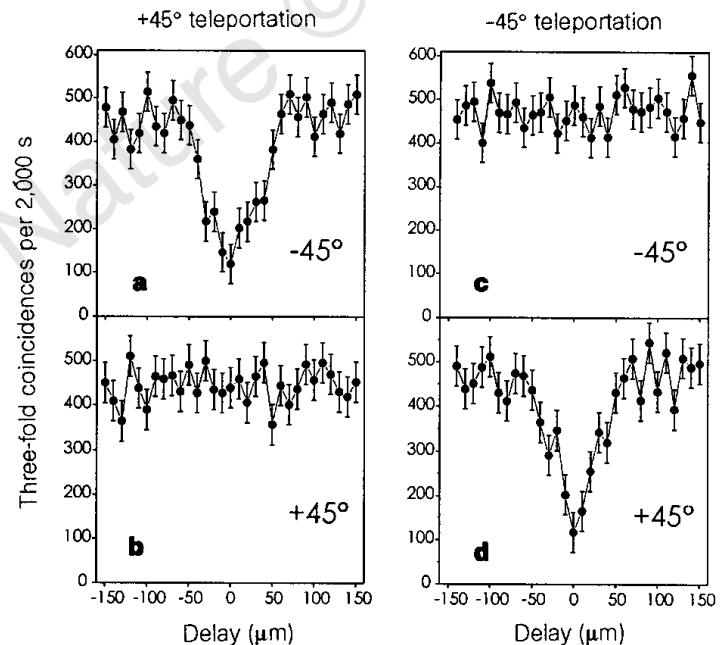
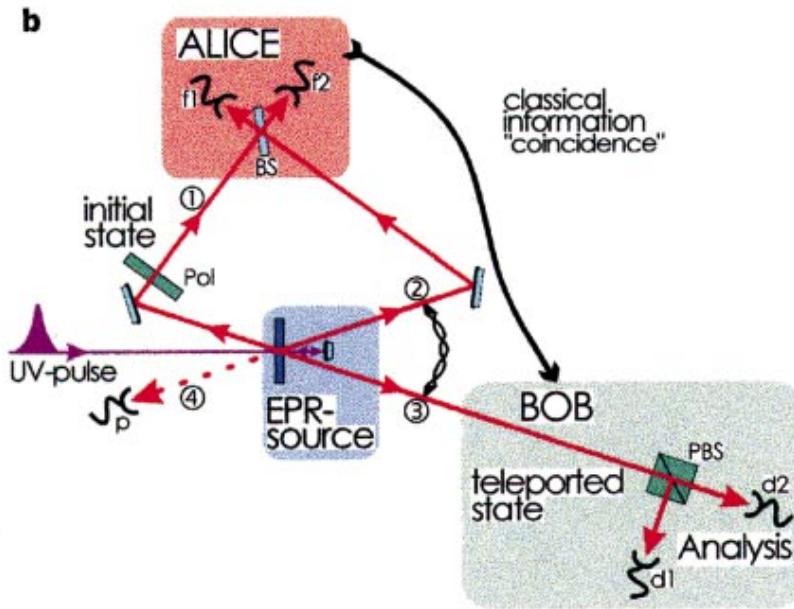
Quantum teleportation with photons

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Institut für Experimentalphysik, Universität Innsbruck, Technikerstr. 25, A-6020 Innsbruck, Austria



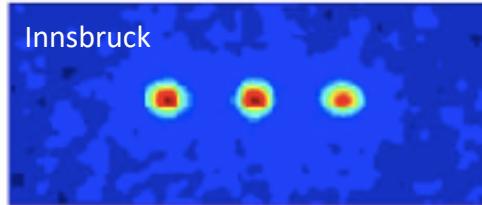
Quantum teleportation with ions (Nature 2005)

Deterministic quantum teleportation of atomic qubits

M. D. Barrett^{1,*}, J. Chiaverini¹, T. Schaetz¹, J. Britton¹, W. M. Itano¹, J. D. Jost¹, E. Knill², C. Langer¹, D. Leibfried¹, R. Ozeri¹ & D. J. Wineland¹

Quantum teleportation¹ provides a means to transport quantum information efficiently from one location to another, without the physical transfer of the associated quantum-information carrier.

${}^9\text{Be}^+$



$$\alpha|\uparrow\rangle + \beta|\downarrow\rangle$$

Deterministic quantum teleportation with atoms

M. Riebe¹, H. Häffner¹, C. F. Roos¹, W. Hänsel¹, J. Benhelm¹, G. P. T. Lancaster¹, T. W. Körber¹, C. Becher¹, F. Schmidt-Kaler¹, D. F. V. James² & R. Blatt^{1,3}

